

From HFT to Laplace Demon

When timed data technology
curves the market



@abifet



@erichoresnyi

HFT in the hey days

High Frequency Trading

5ms=20m\$

Source: Tabb Group

\$100trn

HFT context

Rank	Manager	Market	Assets (US\$million)
1	BlackRock	US	\$4,651,896
2	Vanguard Group	US	\$3,148,496
3	State Street Global	US	\$2,448,112
4	Allianz Group	Germany	\$2,189,296
5	Fidelity Investments	US	\$1,974,077
6	J.P. Morgan Chase	US	\$1,748,849
7	Bank of New York Mellon	US	\$1,710,282
8	AXA Group	France	\$1,491,394
9	Capital Group	US	\$1,396,777
10	Deutsche Bank	Germany	\$1,262,884
11	Goldman Sachs Group	US	\$1,178,000
12	Prudential Financial	US	\$1,175,947
13	UBS	Switzerland	\$1,158,763
14	BNP Paribas	France	\$1,114,595
15	Legal & General Group	UK	\$1,077,425
16	Amundi	France	\$1,052,587

Fidelity
StateStreet
GS
JPM
BoNY
Prudential
Vanguard

Blackrock*
Pimco
CapGroup

*Blackrock is actually headquartered in NY, main AUM coming from ETF/passive originally BGI in SF

AUM>\$1trn, source: Towers Watson

Approx 3xGDP in USA ie 155k\$/hab



Liquidity Flow

HFT context

Buy Side 1



Sell Side 1

PCX

NASDAQ

NSX

NYSE

Sell Side 2



70% Algo

Buy Side 2

Order Flow

HFT context



Sell Side 1



Market Maker



Sell Side 2

Cambrian Explosion

HFT context



ARCA
CME
CBOE
CBOT

NASDAQ
IEX
BRUT
NYSE
INET
NYMEX

BATS

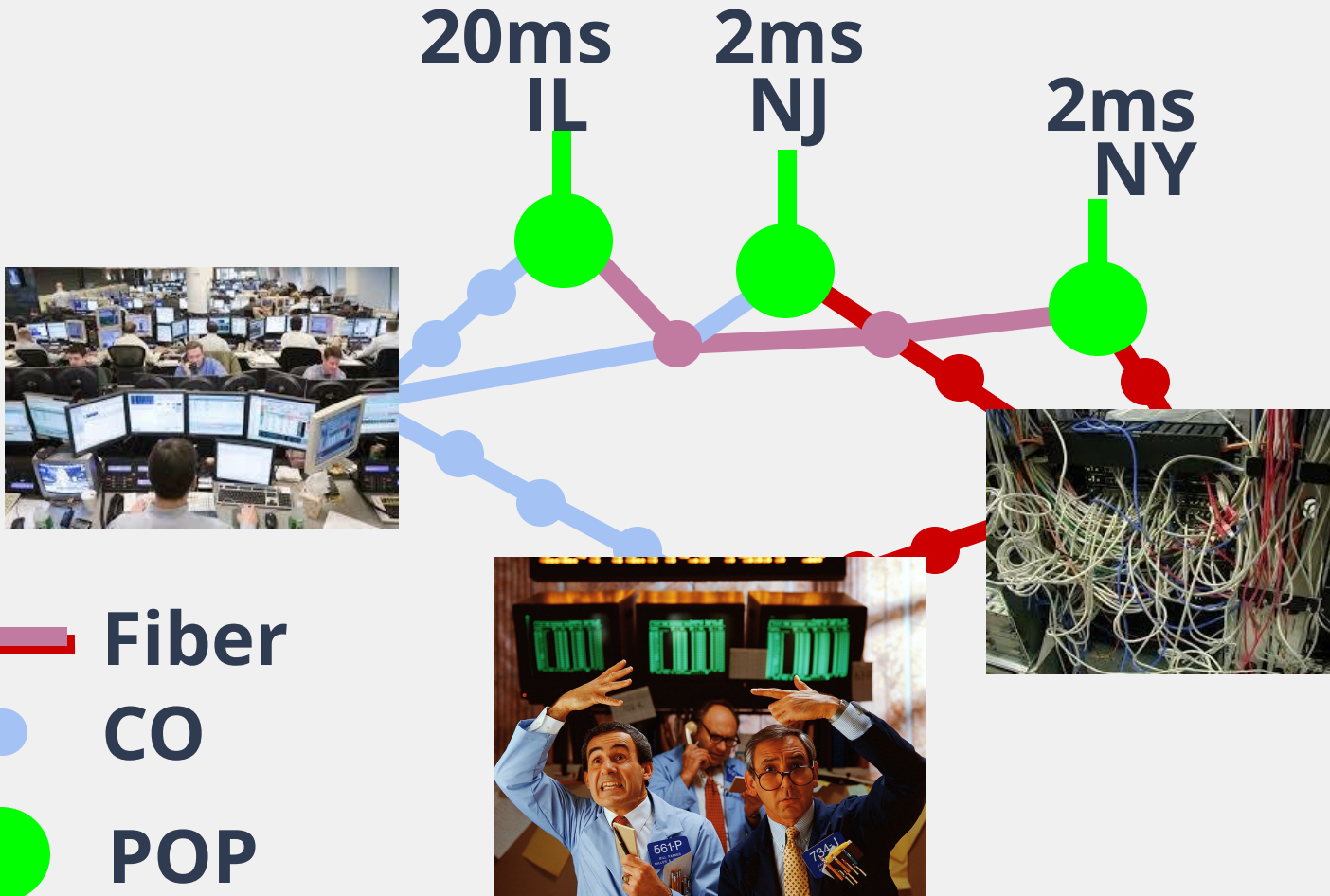
ICE

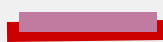


Reg.ATS'98-Reg.NMS'05

PCX

Infra view

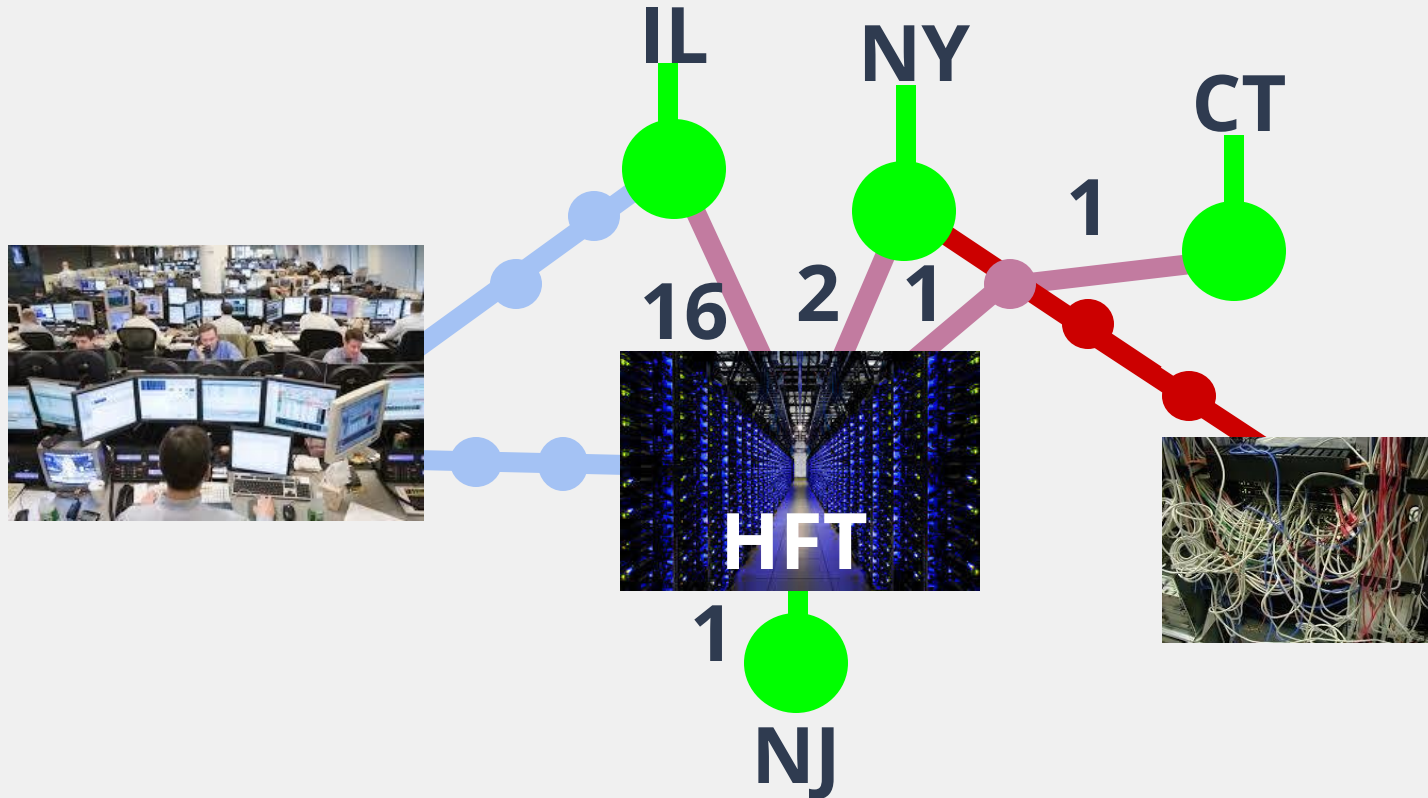
HFT context

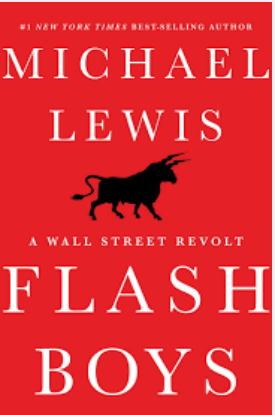


-  Fiber
-  CO
-  POP

HFT: Proximity

Host in Network Nodes, then Exchanges





Latency
=
Propagation
+
Serialization
+
Processing



#1 NEW YORK TIMES BEST-SELLING AUTHOR

MICHAEL
LEWIS



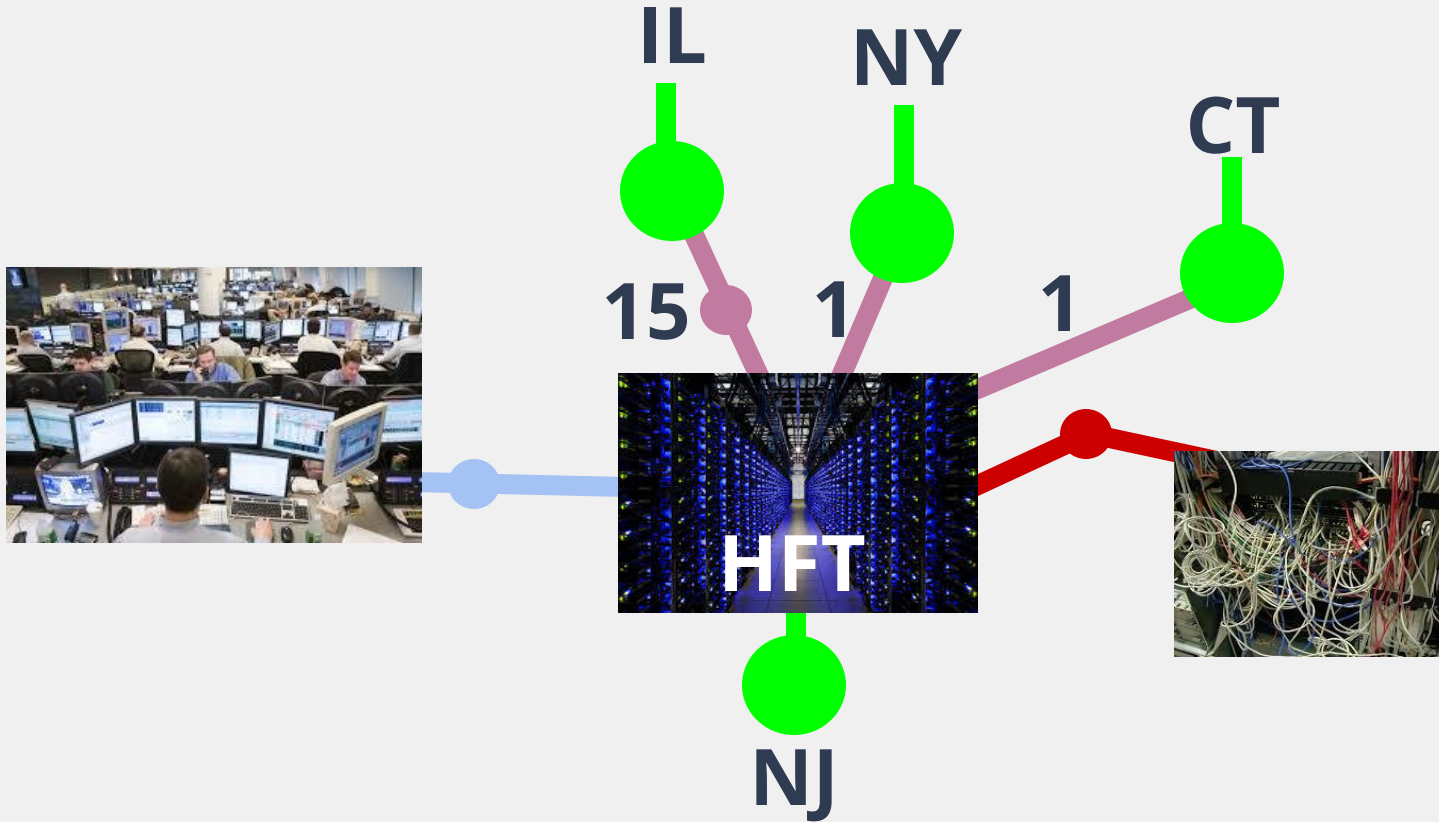
A WALL STREET REVOLT

FLASH
BOYS



HFT: Ultra

Dark Fiber



Buy-Side view of HFT



It's not a ghost...



HFT: Straight Fiber

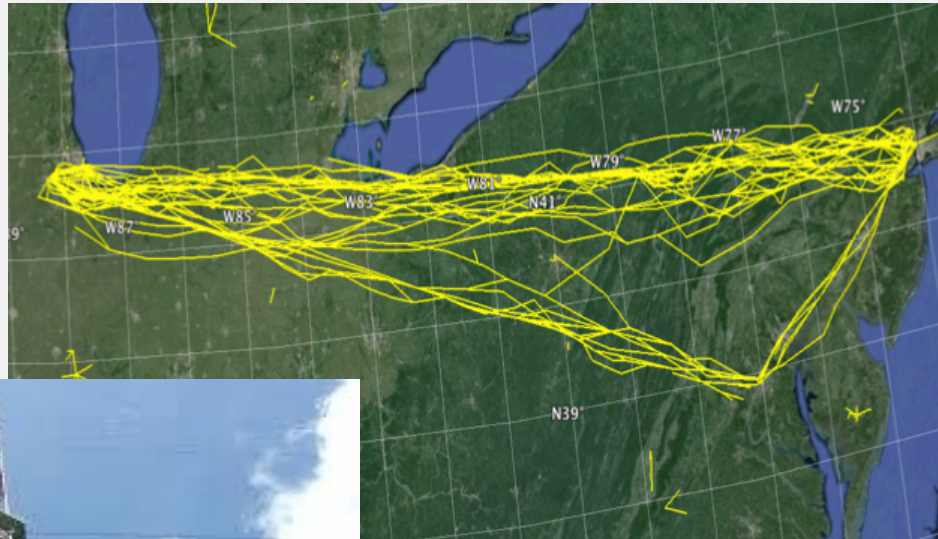
1,000 miles > 825 miles

14.5 ms > 11.5 ms



HFT: Microwaves

$11.5 > 8.5\text{ms}$
 $N:1.33 > 1.0003$
 $v = c/n$



HFT: FPGA

Nanosecs



Choose your lane

HFT <> Algo Trading

"Once you get into milliseconds it's almost not HFT any more"



Spacetime is relative

Market Events: [ct,x,y,z]



Speed curves spacetime

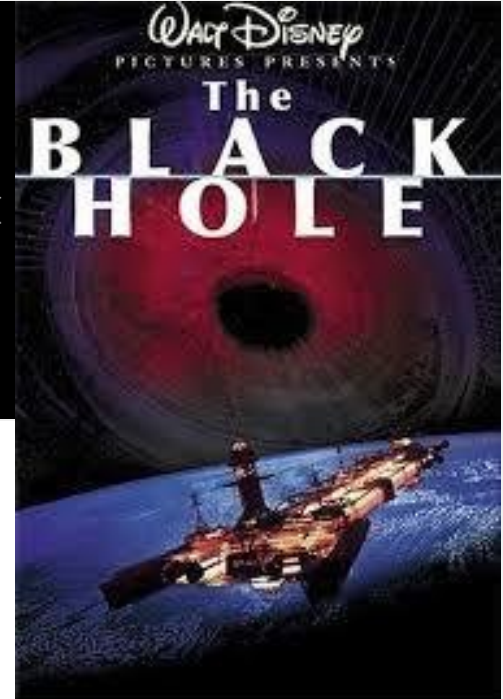
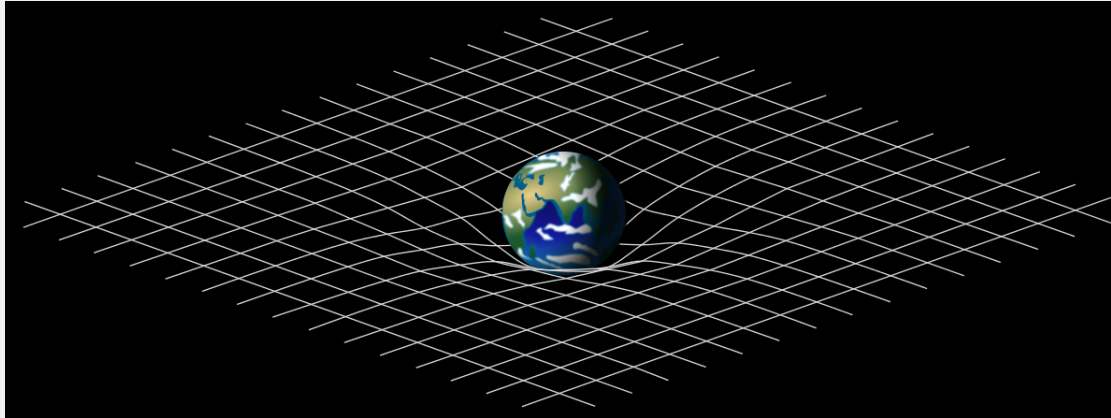
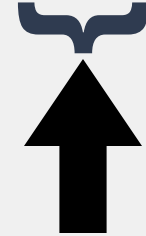
HFT built a wormhole to win on $[ct',x,y,z]$ events



$$\Delta t' = \frac{\Delta t}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Mass curves spacetime

AI builds a blackhole by massively processing [ct,x,y,z] events

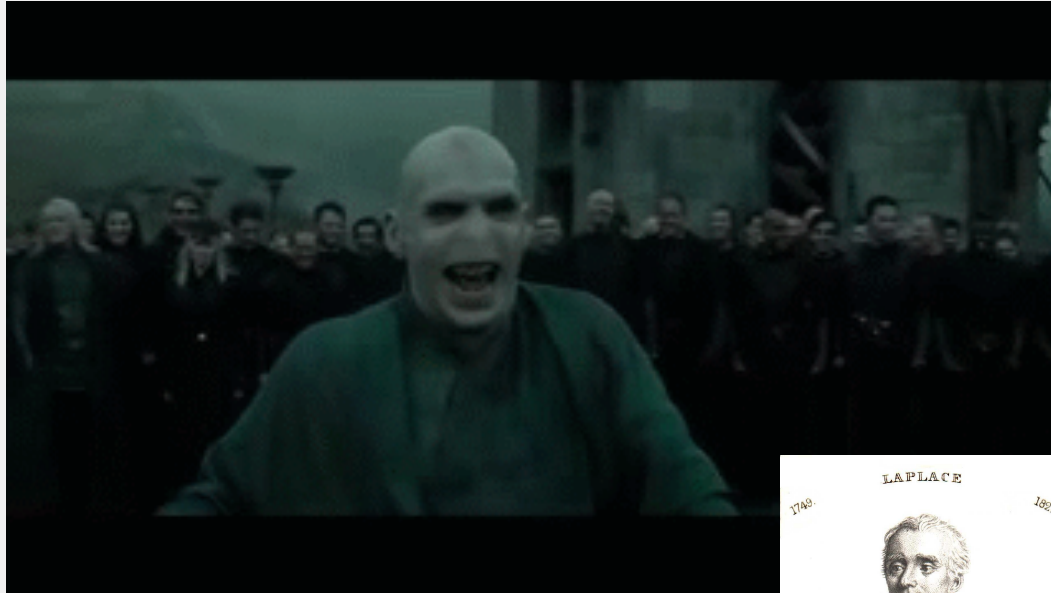


$$G_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Laplace Demon

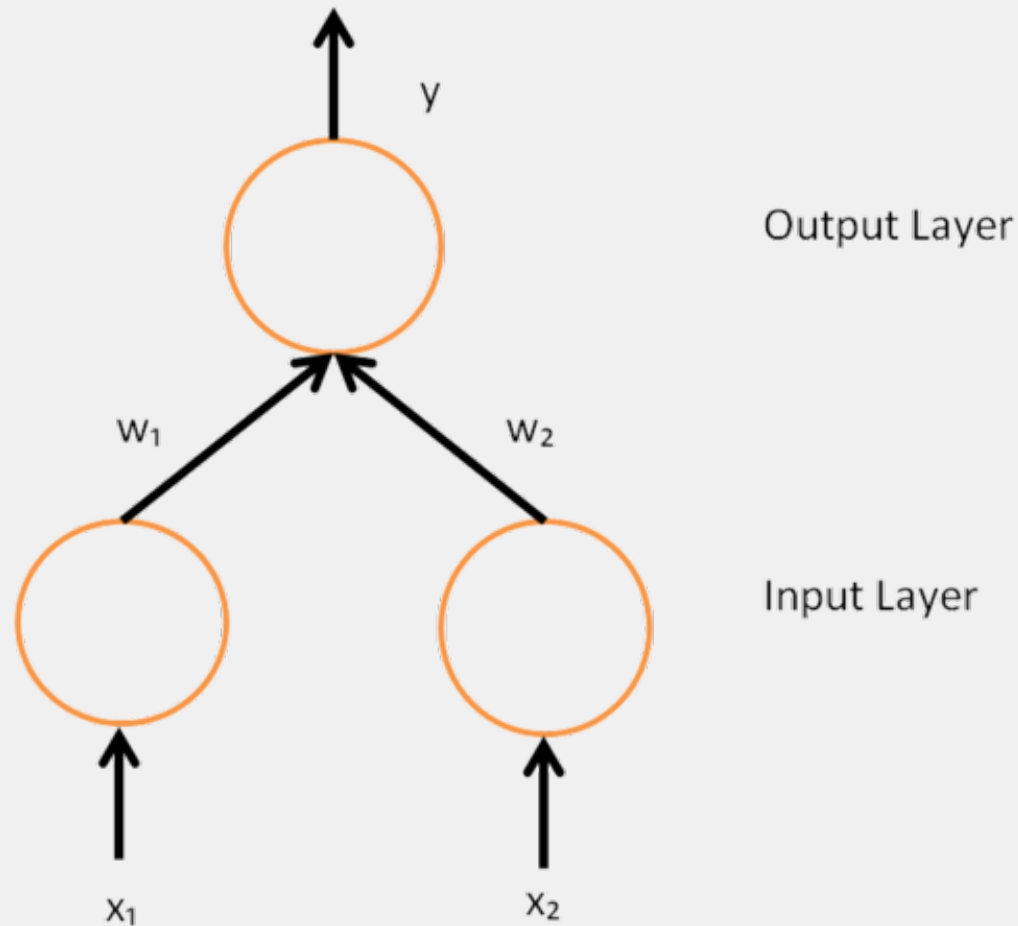
The endgame of Determinism

$$\forall [ct, x, y, z] \in \mathbf{R}^n \vdash \forall [ct', x', y', z']$$



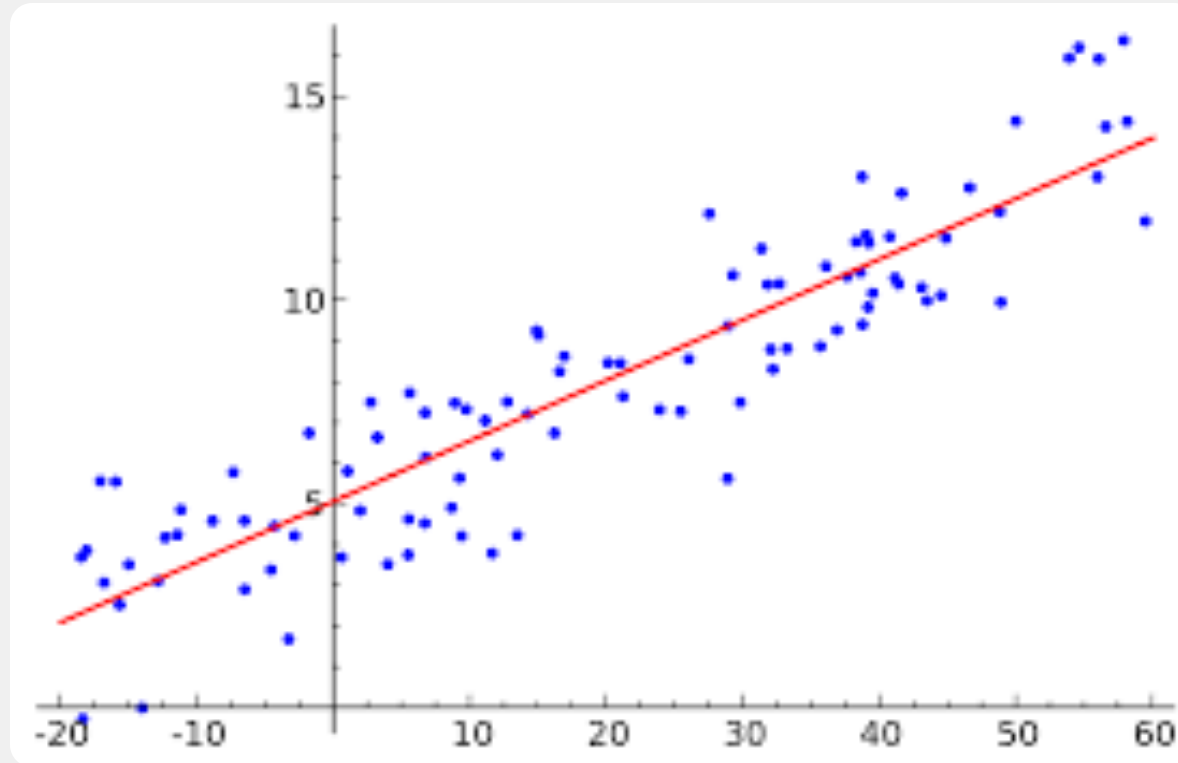
The Endgame 1/3

Event Machine View



The Endgame 2/3

Graph View : Regression

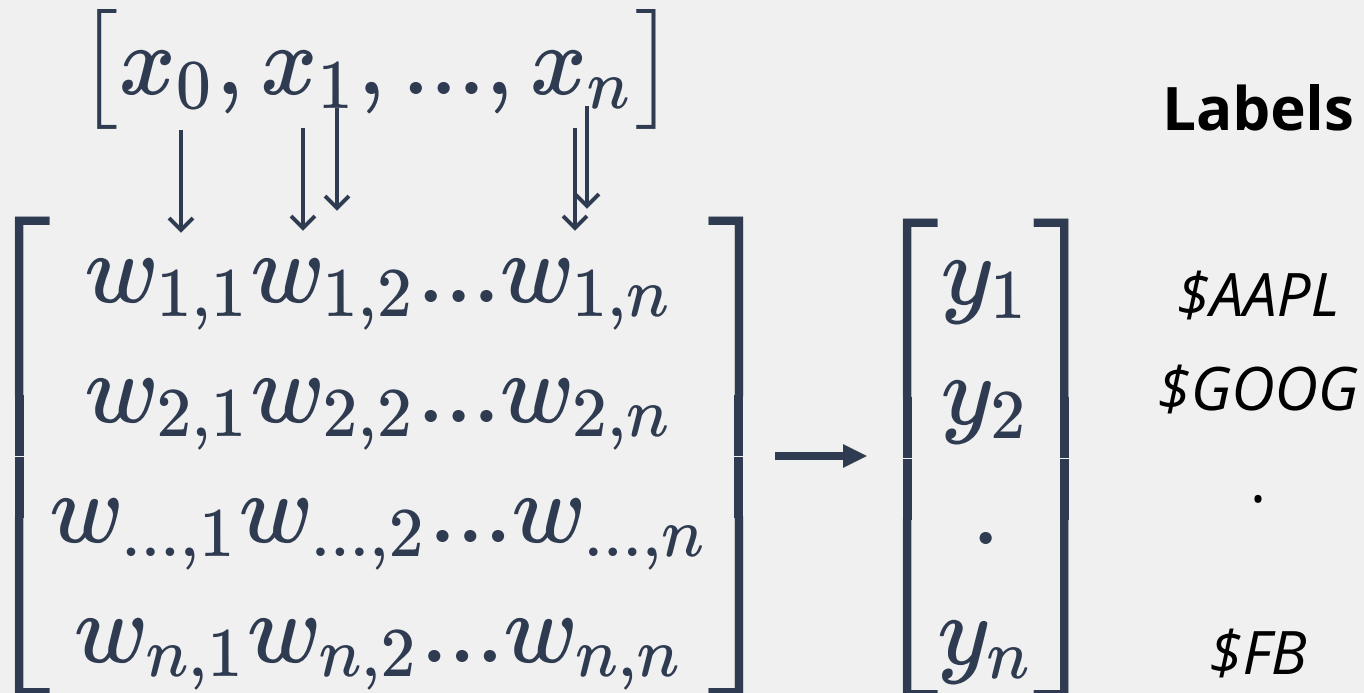


Loss aka Cost Function = $J(\theta)$: distance points to line

The Endgame 3/3

Matrix view

Features



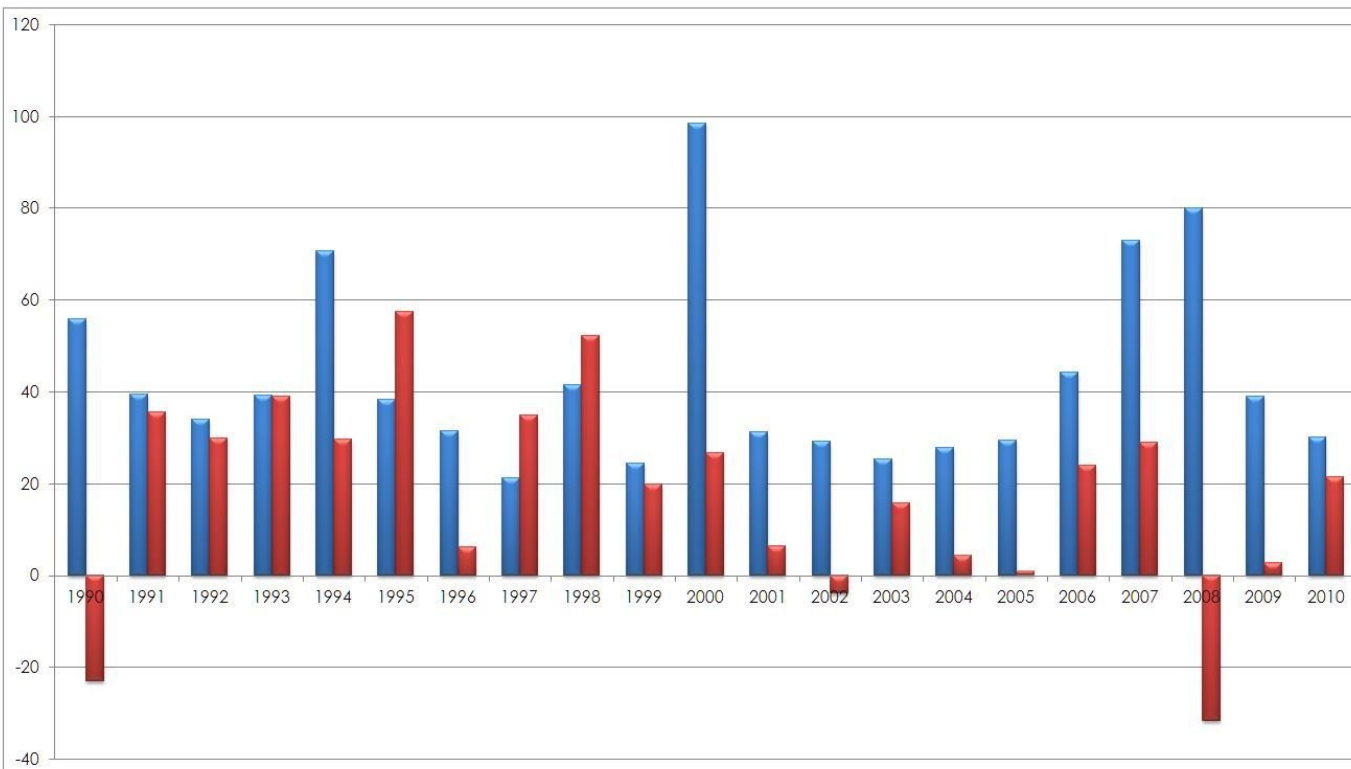
Matrices of Weights

AI not news to trading

+35% yoy for 20 years : \$2,500 > \$1,000,000



■ Medallion Fund
■ BRK

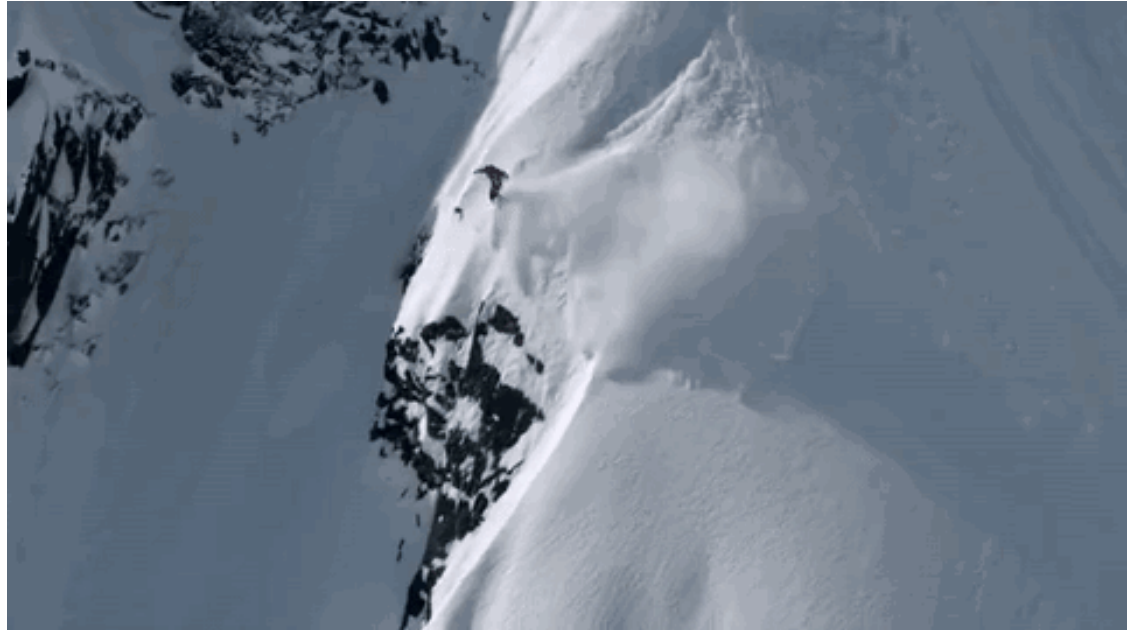
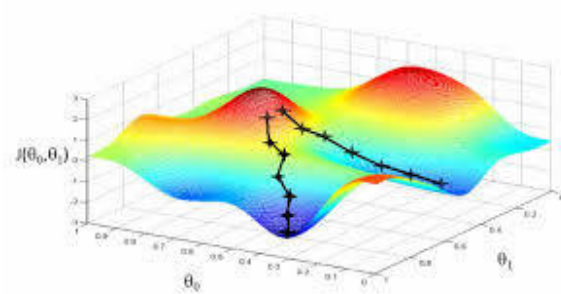


PhD Mathematics, Berkeley - String Theory Chern-Simons Form

AI age: Gradient Descent

Follow the steepest slope, 100m+ features

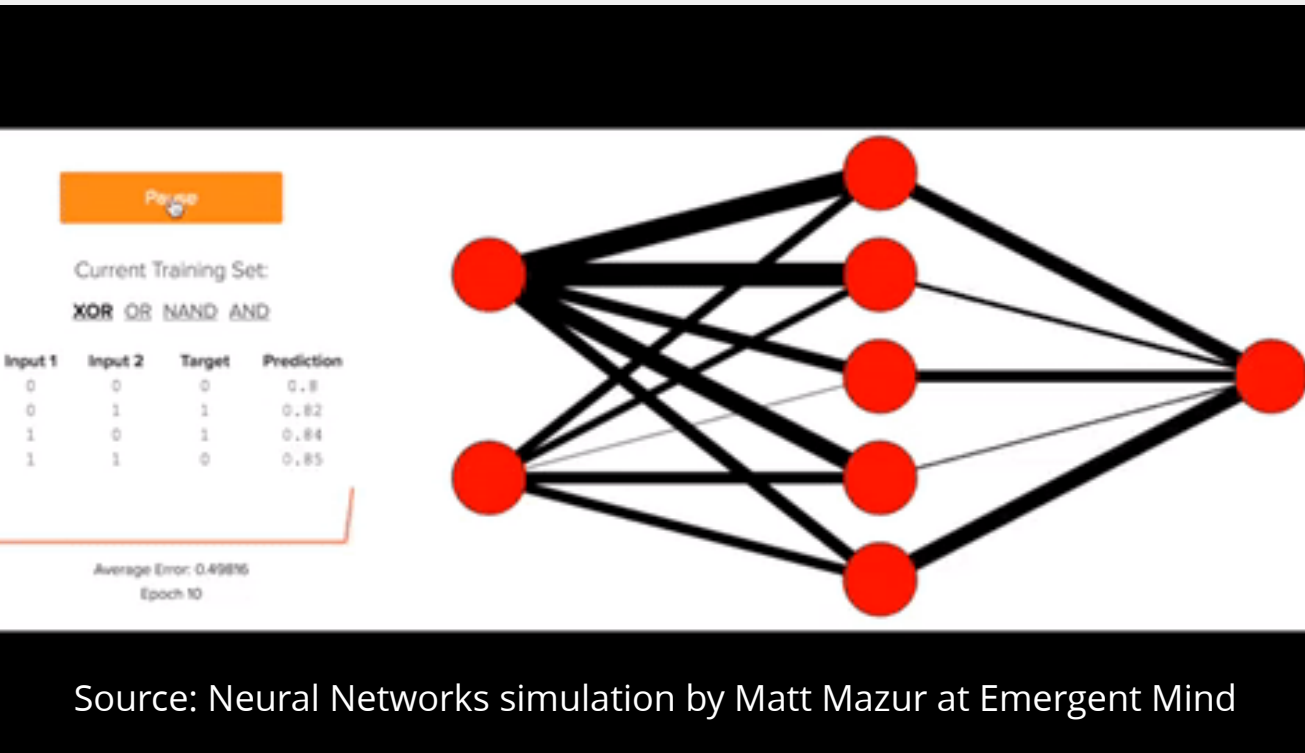
$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta)$$



α : Learning Rate, ∇J : Gradient

AI age: Back Propagation

Adapt weight to control error from previous layer's input, 150+ layers



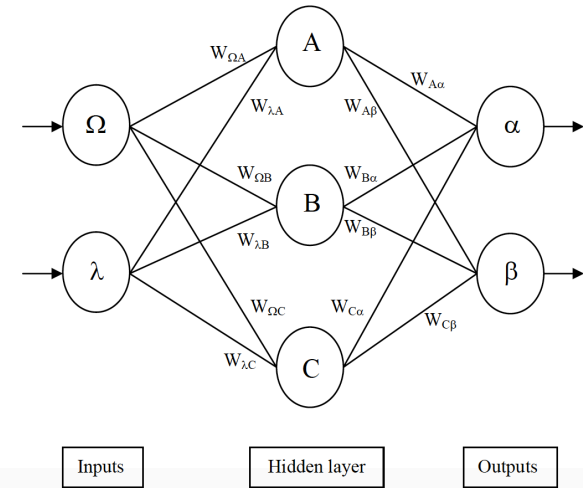
Pause

Current Training Set:
XOR OR NAND AND

Input 1	Input 2	Target	Prediction
0	0	0	0.8
0	1	1	0.82
1	0	1	0.84
1	1	0	0.85

Average Error: 0.49816
Epoch 10

Source: Neural Networks simulation by Matt Mazur at Emergent Mind



AI age: GPU

From Final Fantasy to Autonomous Car



$$\frac{\partial y}{\partial \mathbf{X}} = \begin{bmatrix} \frac{\partial y}{\partial x_{11}} & \frac{\partial y}{\partial x_{21}} & \dots & \frac{\partial y}{\partial x_{p1}} \\ \frac{\partial y}{\partial x_{12}} & \frac{\partial y}{\partial x_{22}} & \dots & \frac{\partial y}{\partial x_{p2}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial y}{\partial x_{1q}} & \frac{\partial y}{\partial x_{2q}} & \dots & \frac{\partial y}{\partial x_{pq}} \end{bmatrix} \cdot$$



"The implementation of streaming algorithms, typied by highly parallel computations with little reuse of input data, has been widely explored on GPUs." (Stanford, 2004)

Bullish Fitness Drill

1-Train



2-Validate



Overfitting?

3-Test



Bearish Fitness Drill

1-Train



2-Validate



Overfitting?

3-Test



Standard Approach

Batch-based, finite training sets, static models

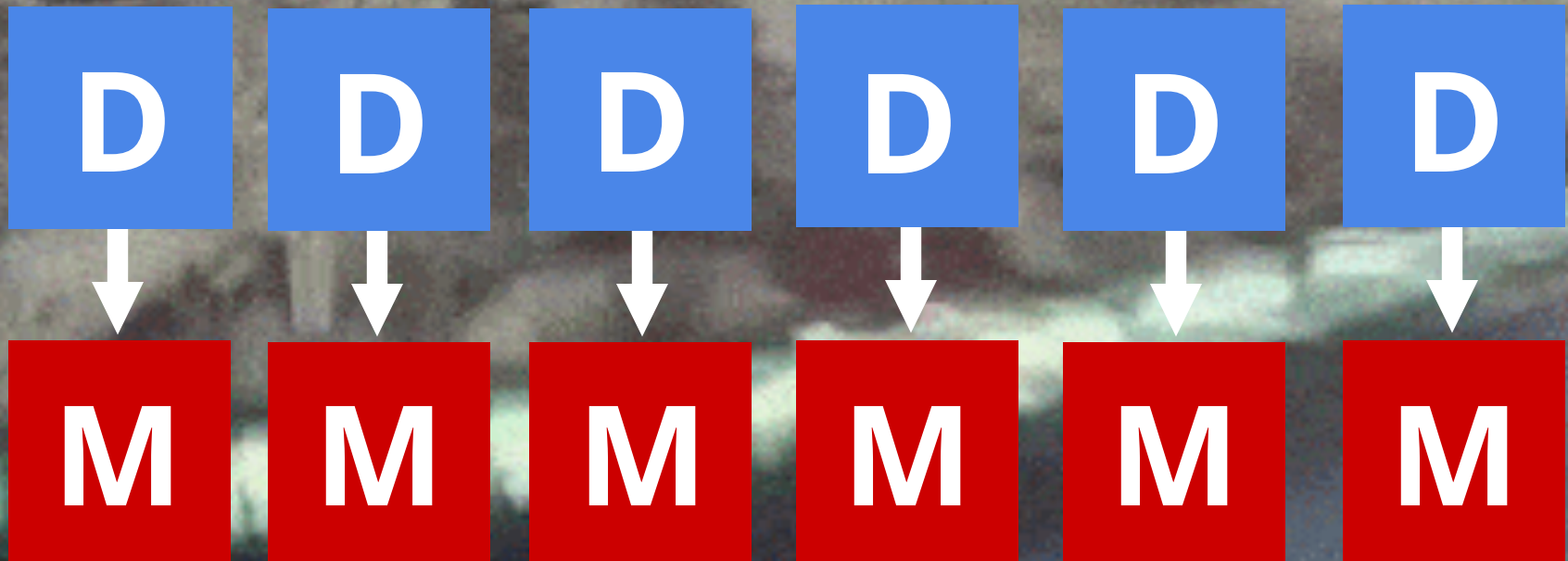


Dataset

Model

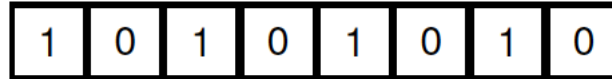
Data Stream Approach

Infinite training sets, dynamic models



Approximation Algo

What is the largest number that we can store in 8 bits?



Programming
Techniques

S.L. Graham, R.L. Rivest
Editors

Counting Large Numbers of Events in Small Registers

Robert Morris
Bell Laboratories, Murray Hill, N.J.

It is possible to use a small counter to keep approximate counts of large numbers. The resulting expected error can be rather precisely controlled. An example is given in which 8-bit counters (bytes) are used to keep track of as many as 130,000 events with a relative error which is substantially independent of the number n of events. This relative error can be expected to be 24 percent or less 95 percent of the time (i.e. $\sigma = n/8$). The techniques could be used to advantage in multichannel counting hardware or software used for the monitoring of experiments or processes.

Approximation Algo

What is the largest number that we can store in 8 bits?

MORRIS APPROXIMATE COUNTING ALGORITHM

- 1 Init counter $c \leftarrow 0$
- 2 **for** every event in the stream
- 3 **do** $rand$ = random number between 0 and 1
- 4 **if** $rand < p$
- 5 **then** $c \leftarrow c + 1$

Approximation Algorithm

101100011110101 0111010

Sliding Window

We can maintain simple statistics over sliding windows, using $O(\frac{1}{\epsilon} \log^2 N)$ space, where

- ▶ N is the length of the sliding window
- ▶ ϵ is the accuracy parameter



M. Datar, A. Gionis, P. Indyk, and R. Motwani.

Maintaining stream statistics over sliding windows. 2002



**Massive
Online
Analysis**

Stream Setting



Process an example at a time

Inspect it only once (at most)

Use a limited amount of memory

Work in a limited amount of time

Be ready to predict at any point

Prequential Evaluation

Sequence of examples \succ Error of a model



$$S = \sum_{i=1}^n L(y_i, \hat{y}_i).$$

Command Line



```
java -cp .:moa.jar:weka.jar -javaagent:sizeofag.jar moa.DoTask  
EvaluatePrequential
```

```
-l DecisionStump //training DecisionStump classifier ...
```

```
-s generators.WaveformGenerator //...on WaveformGenerator data
```

```
-n 100000 //using the first 100 thousand examples for testing
```

```
-i 100000000 //training on a total of 100 million examples
```

```
-f 1000000 //testing every one million examples
```

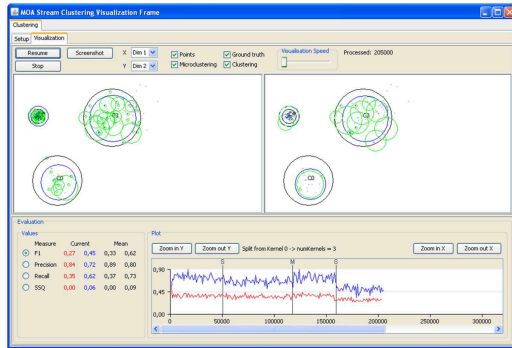
```
> dsresult.csv
```



Resourceful

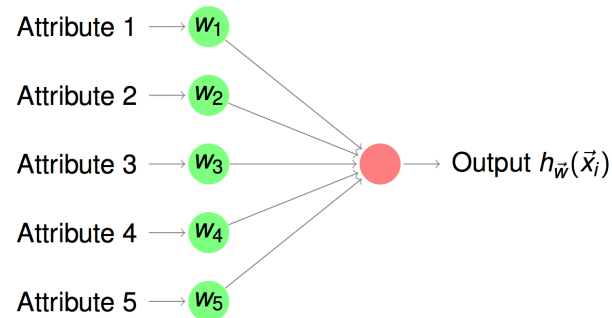


Classification



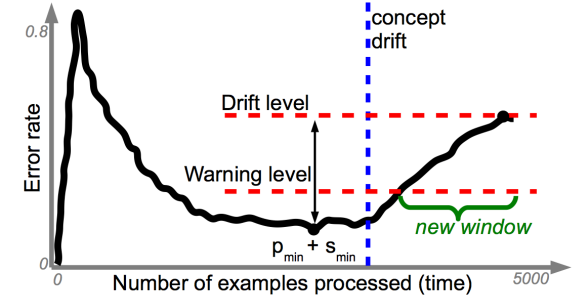
Sentiment Analysis

Regression



Stock Price

Concept Drift



Alerting

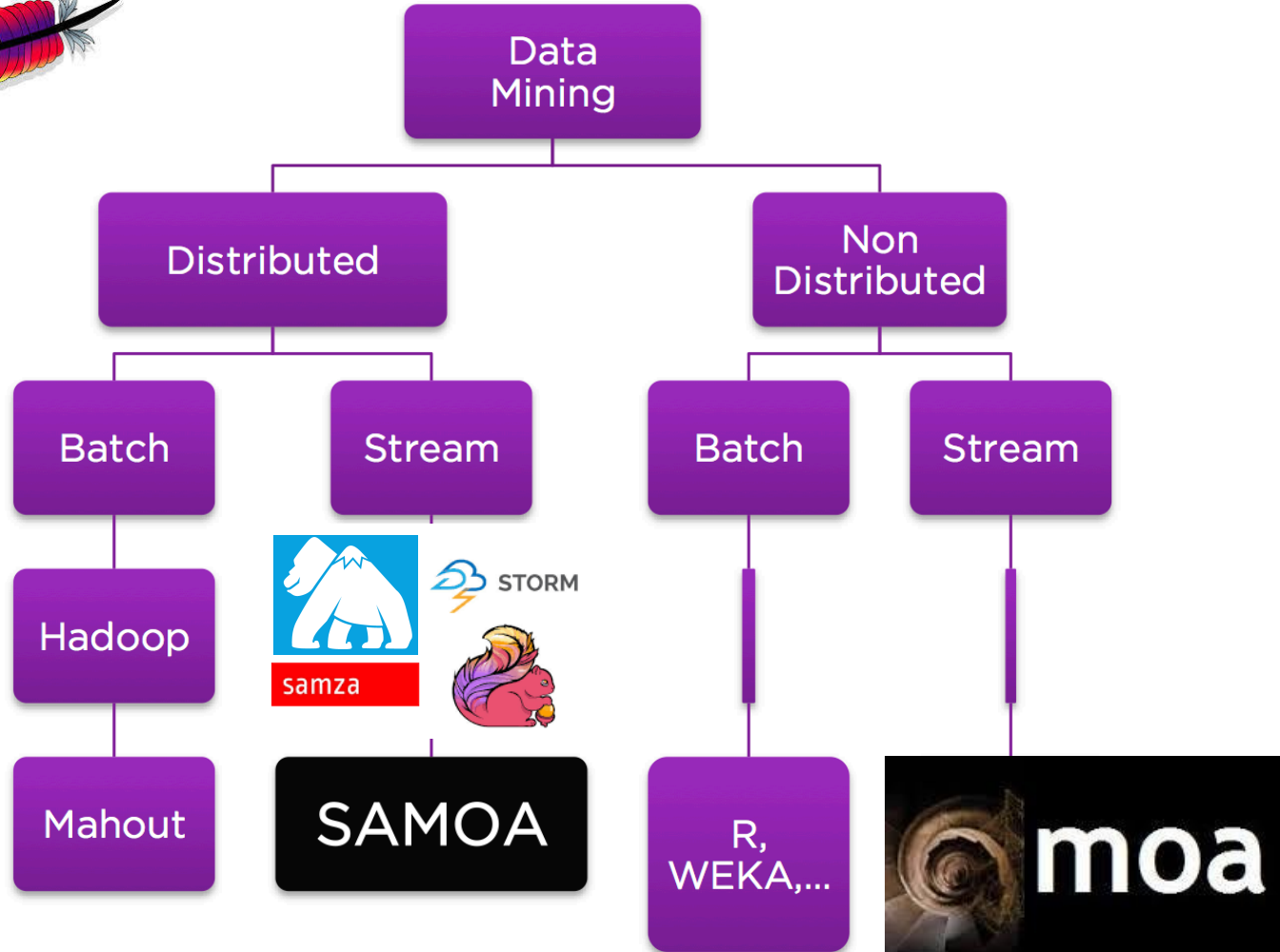
Simple



```
learner.getVotesForInstance(instance)  
learner.trainOnInstance(instance)
```

Scalable

<http://samoa-project.net>



An experiment

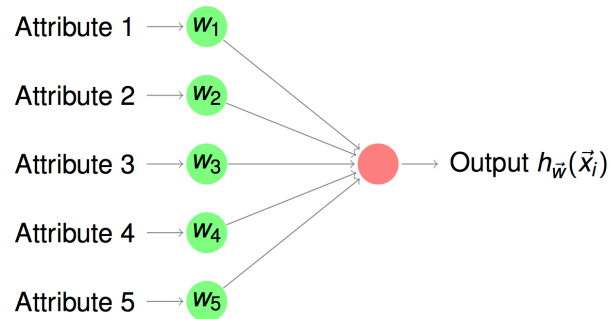


Public Stock Dataset

Name	Price	Time	+/-	Change
HOME DEPOT	71.18 \$	9:47:05	▲	2.95 %
AT&T	36.71 \$	9:47:00	▲	4.88 %
ALCOA	8.61 \$	9:47:05	▲	1.30 %
BOEING CO	78.91 \$	9:47:01	▼	-7.17 %
HEWLETT PACKARD	22.42 \$	9:46:54	▼	-4.20 %
CISCO SYSTEMS	21.52 \$	9:47:05	▲	5.50 %
TRAVELERS COMPANIES (THE)	88.50 \$	9:46:59	▲	6.47 %
UNITEDHEALTH GROUP	56.06 \$	9:46:53	▼	-0.56 %
BANK OF AMERICA	13.13 \$	9:47:05	▲	9.43 %

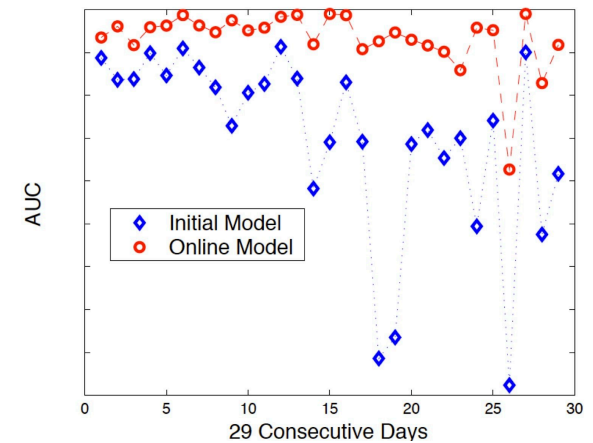


MOA Regression



↓
Stock Price

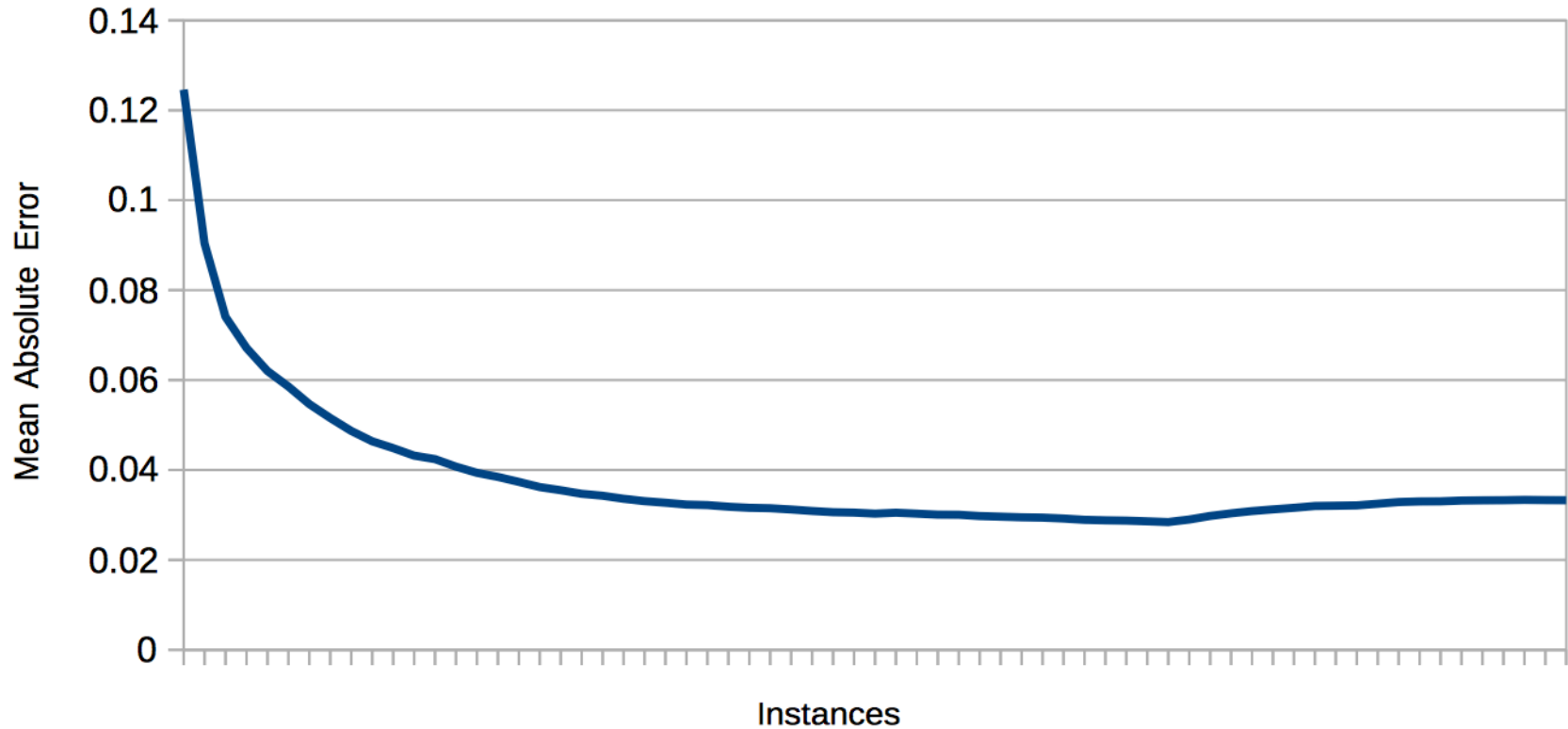
Error



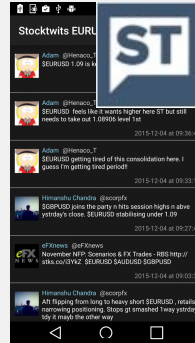
An Experiment



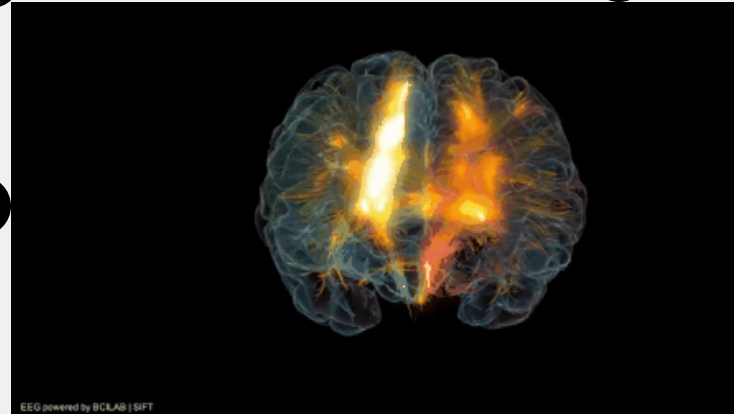
Regression



The New HF Frontier: AI



Sentiment Analysis



Alerts

{API}

Regression/Perceptron



Fast vs Smart

Data Stream a compromise



ct

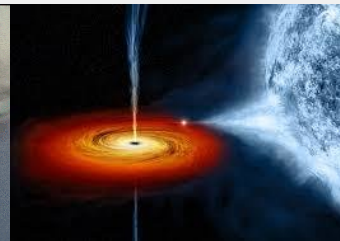
x,y,z



HFT



Data Stream



AI

Thanks!

Apache & Wikipedia Foundation : please donate!

MOA, Kaggle & Giphy : please contribute!

Books & Lectures

Data Stream Mining, MOA team

Yann LeCun Deep Learning Class, NYU

Matt Mazure, Emergent Mind & Andrew Ng, Coursera on AI

My Life as a Quant: Reflections on Physics & Finance, E. Derman

The Value of a Millisecond: Finding the Optimal Speed of a Trading Infra., TabbGroup

Flashboys, M. Lewis

Movies & Games

The Big Short, Back to the Future, Interstellar, The Black Hole,

Harry Potter, Rocky, Into the Mind, Star Wars, Matrix; Final Fantasy

